The Algorithmics of Write Optimization

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Birds-eye view of data storage



Birds-eye view of data storage



Storage systems face a trade-off between the speed of inserts/deletes/updates and the speed of queries.







Like a librarian?



Like a librarian?



Fast to find stuff. Requires work to maintain.

Like a librarian?



Like a teenager?



Fast to find stuff. Requires work to maintain.

Like a librarian?



Like a teenager?



Fast to find stuff. Requires work to maintain. Fast to add stuff. Slow to find stuff.

Like a librarian?



Like a teenager?



Fast to find stuff. Requires work to maintain.

"Indexing"

Fast to add stuff. Slow to find stuff. "Logging"



(**8**,1)

Find a key: fast. Insert a key: slower. Find a key: slow. Insert a key: fast.

(4,3)



Find a key: fast. Insert a key: slower. Find a key: slow. Insert a key: fast.





Find a key: fast. Insert a key: slower. **logging** Sort in arrival order.



Find a key: slow. Insert a key: fast.



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 unclustered indexes



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 unclustered indexes
- in-place file systems log-structured file systems
- etc!



DBs, kv-stores, and file systems are different beasts.

But they grapple with the similar data-structures problems.

SQL database	noSQL database	file system
SQL processingquery optimization	 key-value operations 	 file and directory operations
persistent data structure	persistent data structure	persistent data structure
	Disk/SSD	

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Similar problems \Rightarrow similar solutions

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Some "write-optimized" data structures can mitigate or overcome the indexing-logging trade-off.

At our DB company Tokutek,* we sold open-source write-optimized databases.

Since it was sold, we've built an open-source file system.

TokuDB SQL database	TokuMX noSQL database	BetrFS file system
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I'll talk about my experiences using the		

Disk/SSD

experiences using the same data structure to help all three systems.

*acquired by Percona

The performance landscape is fundamentally changing.

- New data structures
- New hardware



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This has created tons of new research opportunities.

- For algorithmists/theorists
- For systems builders



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There's still lots to do.

An algorithmic view of the insert-query tradeoff

Performance characteristics of storage



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Sequential access is fast.



Performance characteristics of storage Sequential access is fast. Random access is slower. J 398 10 MB U'SIDINIO UNDER! YOU'VE BEEN WAITING FOR included with the system is software for testing. mattero, LO drivers for CP/M*, plus an automati-

inte micro size disk

which program. Support software and

A model for I/O performance

How computation works:

- Data is transferred in blocks between RAM and disk.
- The # of block transfers dominates the running time.

Goal: Minimize # of I/Os

• Performance bounds are parameterized by block size **B**, memory size **M**, data size **N**.



Disk-Access Machine (DAM) model [Aggarwal+Vitter '88]

I/Os are slow

RAM: ~60 nanoseconds per access Disks: ~6 milliseconds per access. Analogy:



- RAM \propto escape velocity from earth (40,250 kph)
- disk \propto walking speed of the giant tortoise (0.4 kph)





How realistic is the DAM model?


"All models are wrong, but some are useful"





[George Box 1978]

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• Unrealistic in various ways.

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- Great for reasoning about I/O and for high-level design.

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- Unrealistic in various ways.
- Great for reasoning about I/O and for high-level design.
- You can optimize the model to hone constants.

A model for I/O performance

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Disk-Access Machine (DAM) model [Aggarwal+Vitter '88]

I/O cost for logging.



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• query: scan all blocks $\Rightarrow O(N/B)$



I/O cost for logging.

- query: scan all blocks $\Rightarrow O(N/B)$
- insert: append to end of log $\Rightarrow O(1/B)$



Q: What's the I/O cost for indexing? A: It depends on the indexing data structure.

The classic indexing structure is the B-tree.



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Queries: O(log_BN) Inserts: O(log_BN)

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Beating B-tree Bounds



Goal:

Inserts that run faster than a B-tree. Queries that don't run slower.

Beating B-tree Bounds



Start with a regular B-tree





Reduce the fanout.

• Now the nodes are mostly empty





Put $B^{1/2}$ -sized buffers in each internal node.



- Send insert/delete messages down from the root and store them in buffers.
- When a buffer fills up, flush.



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Searches cost O(log_BN)

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Insertions analysis in B^ɛ tree

Inserts cost $O((\log_B N)/\sqrt{B})$ per insert/delete.

- Each flush cost 1 I/O and flushes \sqrt{B} elements.
- Flush cost per element is $1/\sqrt{B}$.
- There are $O(\log_B N)$ levels in a tree.



Write-optimization [Brodal, Fagerberg 03]


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Example:

Record size: 128 bytes Node size: 128 KB B: 1024 records Speedup: $\approx \frac{\sqrt{1024}}{2} = 16$

Write-optimization [Brodal, Fagerberg 03]





Optimal insertion-search tradeoff curve

[Brodal, Fagerberg 03]

Optimal Search-Insert Tradeoff [Brodal, Fagerberg 03]

Change the fanout to

from $B^{1/2}$ to B^{ε} .





Illustration of Optimal Tradeoff [Brodal, Fagerberg 03]



Illustration of Optimal Tradeoff [Brodal, Fagerberg 03]



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Illustration of Optimal Tradeoff [Brodal, Fagerberg 03]







insert point query



Write performance on large data



MongoDB

MySQL

Other WODS

Other write-optimized data structures

The most famous write-optimized data structure is the log structured merge tree [O'Neil, Cheng, Gawlick, O'Neil 96]



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Write optimization is having a large impact on systems.

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Write-optimization in databases

ACID-compliant database

application

SQL processing

SQL database

query optimization

database index

(traditionally a B-tree)

file system



ACID-compliant database built on a B^ɛ-tree

application

- SQL processing
- query optimization

SQL database

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ACID-compliant database built on a B^ε-tree



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We built a write-optimized SQL databases at our DB company Tokutek.



ACID-compliant database built on a B^ε-tree

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Write optimization. What's missing?

Everything else

- Variable-sized rows
- Concurrency-control mechanisms
- Multithreading
- Transactions, logging, ACID-compliant crash recovery
- Optimizations for the special cases of sequential inserts and bulk loads
- Compression
- Backup



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Ingredients

• a regular write-optimized structure





periodic checkpoints of the WOD



B-sized buffers

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Ingredients

• a regular write-optimized structure











With TokuDB you can index data 10x-100x faster.





a company

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We don't have an insertion bottleneck. We have a query bottleneck.


















The right read optimization is write optimization



The right index makes queries run fast. WODS can maintain them.

Fast writing is a currency we use to make queries faster.

WODs force you to reexamine your system design...



What the world looks like

Insert/point query asymmetry

- Inserts can be fast: 50-100K random writes/sec on a disk.
- Point queries are provably slow: <200 random reads/sec on a disk.

Systems are often designed assuming reads and writes have about the same cost.

In fact, writing is easier than reading.

Systems often assume search cost = insert cost

Ancillary search—a search with each insert.

- Insert with uniqueness check is the key is already present?
- Delete with acknowledgement was a key actually deleted?



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In a B-tree, the leaf is already fetched, so reading it has no extra cost. In a WOD, it's expensive.

These ancillary searches throttle insertions down to the performance of B-trees.

How can we get rid of ancillary searches?

Write-optimized systems must get rid of or mitigate ancillary searches whenever possible.



It's remarkable that uniqueness checking is hard, but ACID compliance is asymptotically easy.

We now live with a different model for what's expensive and what's cheap.

Using WODs in File Systems

(BetrFS, TokuFS, TableFS are examples of write-optimized file systems. I'll talk about BetrFS)

Using WODs in File Systems

The empirical tradeoff between writing and querying appears in

file systems.

00

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How should we organize the files on disk?



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logical order \Rightarrow sequential scans are fast



- grep -r "bar" .
- Is -R .

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update order \Rightarrow small writes are fast



How should we organize the files on disk?



logical order \Rightarrow sequential scans are fast Updates are slow.

• Is -R .

update order \Rightarrow small writes are fast



How should we organize the files on disk?



directory tree



• Is -R .

update order \Rightarrow small writes are fast



Maintain two WODs, each indexed on the path names.



directory tree

<path, file="" metadata=""></path,>	<path, data="" file=""></path,>
/home/bender/doc	/home/bender/doc
/home/bender/doc/latex/	/home/bender/doc/latex/
/home/bender/doc/latex/a.tex	/home/bender/doc/latex/a.tex
/home/bender/doc/latex/b.tex	/home/bender/doc/latex/b.tex
/home/bender/doc/foo.c	/home/bender/doc/foo.c
/home/bender/local	/home/bender/local

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<path, file="" metadata=""></path,>	<path, data="" file=""></path,>
/home/bender/doc	/home/bender/doc
/home/bender/doc/latex/	/home/bender/doc/latex/
/home/bender/doc/latex/a.tex	/home/bender/doc/latex/a.tex
/home/bender/doc/latex/b.tex	/home/bender/doc/latex/b.tex
/home/bender/doc/foo.c	/home/bender/doc/foo.c
/home/bender/local	/home/bender/local

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/home/bender/doc/latex/	/home/bender/doc/latex/
/home/bender/doc/latex/a.tex	/home/bender/doc/latex/a.tex
/home/bender/doc/latex/b.tex	/home/bender/doc/latex/b.tex
/home/bender/doc/foo	/home/bender/doc/foo.c
/home/bender/local	/home/bender/local

Microwrite and Scan Performance on BetrFs



Microwrite and Scan Performance on BetrFs



[BetrFS: Jannen, Yuan, Zhan, Akshintala, Esmet, Jiao, Mittal, Pandey, Reddy, Walsh, Bender, Farach-Colton, Johnson, Kuszmaul, Porter, FAST 15]

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<path, file="" metadata=""></path,>	<path, data="" file=""></path,>
/homo/hondor/doo	/homo/hondor/doo
/nome/bender/doc	/nome/bender/doc
/home/bender/doc/latex/	/home/bender/doc/latex/
/home/bender/doc/latex/a.tex	/home/bender/doc/latex/a.tex
/home/bender/doc/latex/b.tex	/home/bender/doc/latex/b.tex
/home/bender/doc/foo.c	/home/bender/doc/foo.c
/home/bender/local	/home/bender/local

Some file-system operations don't seem to map cheaply.



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<path, file="" metadata=""></path,>	<path, data="" file=""></path,>
/home/bender/doc	/home/bender/doc
/home/bender/doc/latex/	/home/bender/doc/latex/
/home/bender/doc/latex/a.tex	/home/bender/doc/latex/a.tex
/home/bender/doc/latex/b.tex	/home/bender/doc/latex/b.tex
/home/bender/doc/foo.c	/home/bender/doc/foo.c
/home/bender/local	/home/bender/local

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/home/bender/doc/latex/	/home/bender/doc/latex/
/home/bender/doc/latex/a.tex	/home/bender/doc/latex/a.tex
/home/bender/doc/latex/b.tex	/home/bender/doc/latex/b.tex
/home/bender/doc/foo.c	/home/bender/doc/foo.c
/home/bender/local	/home/bender/local

Some file-system operations don't seem to map cheaply.



These keys change their names. They move to a different place in the order.

WODs open questions



Moral: how can we make write-optimized data structures that support the richer set of operations needed by the applications?

We need more than just insert and delete.

Other WODs advantages

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B^ɛ-trees can use bigger nodes than B-trees

- Better compression
- Less fragmentation.

B^ɛ-trees file systems do not age the way **B**-tree based file systems do.

[Conway, Bakshi, Jiao, Zhan, Bender, Jannen, Johnson, Kuszmaul, Porter, Yuan, Farach-Colton 17]



optimize

ree
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[Conway, Bakshi, Jiao, Zhan, Bender, Jannen, Johnson, Kuszmaul, Porter, Yuan, Farach-Colton 17]



Revisit I/O model to harness full power of write-optimization

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Some things it doesn't predict, such as aging.

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Technology is changing.

- I/O speeds are accelerating faster than CPU.
- Storage technology supports lots of I/Os in parallel.

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Some things it doesn't predict, such as aging.

Technology is changing.

- I/O speeds are accelerating faster than CPU.
- Storage technology supports lots of I/Os in parallel.

Need multithreading and lots of parallel I/Os to drive the device to its capacity.

• Data structures for older storage don't work so well now.





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We should rethink applications and the storage stack given new write-optimized data structures.

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WODS are accessible. They are teachable in standard curricula.

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We should revisit the performance model. To get performance now we need parallelism everywhere.